Elementary processes governing the evolution of road networks

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Urbanisation is a fundamental phenomenon whose quantitative characterisation is still inadequate. We report here the empirical analysis of a unique data set regarding almost 200 years of evolution of the road network in a large area located north of Milan (Italy). We find that urbanisation is characterised by the homogenisation of cell shapes, and by the stability throughout time of high–centrality roads which constitute the backbone of the urban structure, confirming the importance of historical paths. We show quantitatively that the growth of the network is governed by two elementary processes: (i) 'densification', corresponding to an increase in the local density of roads around existing urban centres and (ii) 'exploration', whereby new roads trigger the spatial evolution of the urbanisation front. The empirical identification of such simple elementary mechanisms suggests the existence of general, simple properties of urbanisation and opens new directions for its modelling and quantitative description.

Urbanisation is a fundamental process in human history [1], and is increasingly affecting our environment [2] and our society [3–5]. The fraction of the world population living in urban areas has recently grown beyond 50% and is expected to rapidly increase in the near future [6]. The challenges presented by such a rapidly urbanising world are complex and difficult to handle. They range from the increasing dependence of our society on fossil fuels [7], to the emergence of socio-spatial inequalities [8, 9], and to the up-rise of serious environmental issues [10]. Controlling urbanisation has already proven to be a difficult task, and it will become even more difficult in the near future, due to the large and unprecedented magnitude of urban expansion [11], and to the intrinsic complexity of this phenomenon, which generates cities that are continuously changing over time [12] in a non-homogeneous fashion [13]. Trying to understand the elementary spatial mechanisms that govern urbanisation, leaving out specific historical, geographical, social and cultural factors, is nowadays more important than ever, especially because policy makers, professionals and researchers are actively looking for new paradigms in urban planning, land management and ecology [14–16]. The existence of acultural and non-demographic drivers of urbanisation has been investigated using different approaches [17], including classical studies in regional sciences [18], theory of complex systems [19–21], urban theory [22] and remote sensing [23]. A consistent amount of literature in urban history and morphology indicates that roads are a fundamental driver in urban evolution and, at the same time, one of the long-lasting constituent elements of urban forms [24, 25]. In the last decade, complex networks theory has provided significant contributions to the quantitative characterisation of urban street patterns [27–29]. Several studies have shown that road networks not only play a central role in the spatial organisation of urban areas [30, 31], but are important for the dynamical processes occurring on them [29, 32–35] and for the evolution of urban systems in general [36, 37]. However, a quantitative analysis of the historical development of urbanisation in metropolitan areas is still missing, and empirical evidence of the basic mechanisms governing urbanisation dynamics is still lacking. Our paper addresses this problem, and provides a study of the evolution over two centuries of the road network in a large urban area located north of Milan (Italy).

The area under study, known as *Groane*, covers a surface of 125 km^2, includes 29 urban centres within 14 municipalities, and has essentially evolved along two main radial paths, connecting Milan to Como and Milan to Varese, respectively. The former path was constructed by the Romans during the II century B.C., while the latter was created during the XVI century. In the last two centuries, the Groane area has faced a complex process of conurbation, changing from a polycentric region into a completely urbanised area. This conurbation process is common to many large European metropolitan regions [38]. Despite local differences, it is possible to identify four distinct phases that characterize urbanization in the Groane area: i) *Rural phase*, (1800-1918): fundamentally pre-industrial, fully based on agricultural economy, with no major transportation infrastructures
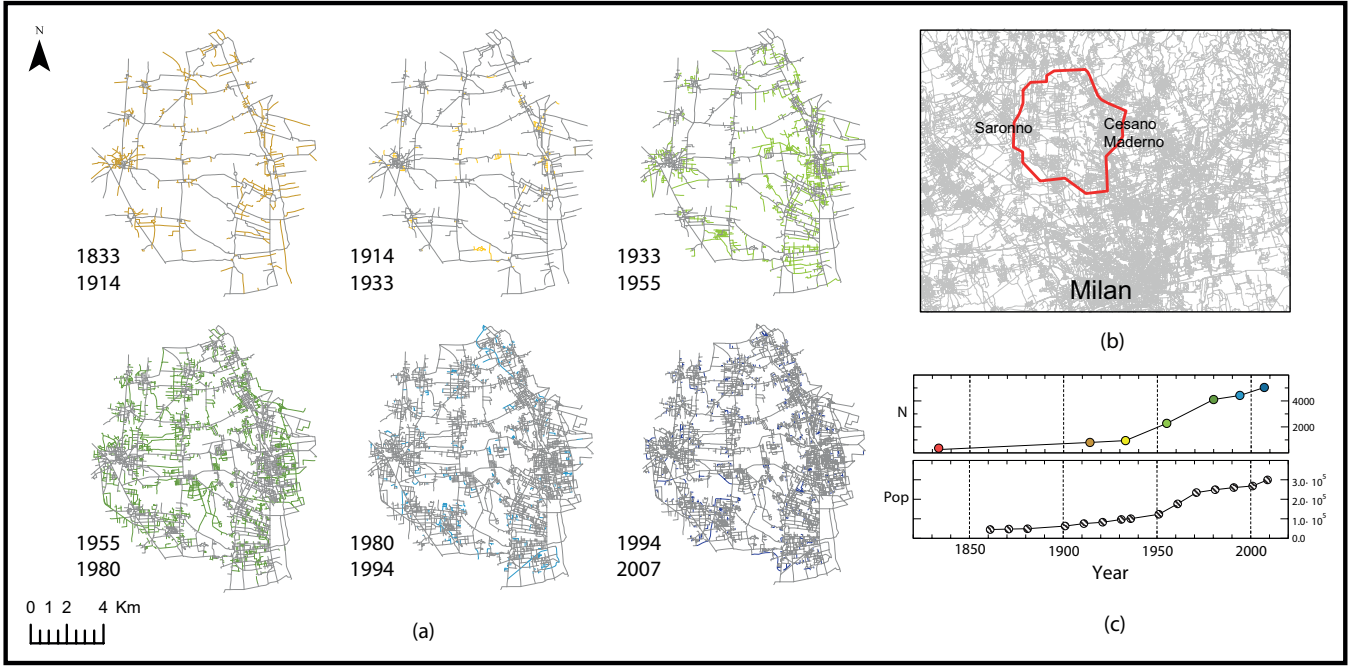
FIG. 1. **(a)** Evolution of the road network from 1833 to 2007. For each map we show in grey all the nodes and links already existing in the previous snapshot of the network, and in colors the new links added in the time window under consideration. **(b)** Map showing the location of the Groane area in the metropolitan region of Milan. **(c)** Time evolution of the total number of nodes N in the network and of the total population in the area (obtained from census data).

present. ii) *Early-urban phase* (1918-1945): between world wars period, still significantly based on agriculture economy, witnessing the first appearance of rail network, first small-scale sparse industrial colonisation, and limited expansion of rural settlements around the historical centres. iii) *Urban-industrial phase* (1945-1990): remarkable sprawled residential and industrial development (especially textile and mechanics) along with population growth and highway construction. iv) *Metropolitan post-industrial phase* (1990- 2012): decline of industrial activities, slower-paced urban sprawl, former polycentric organisation overwhelmed by the metropolitan continuum caused by the merging of expanded centres, increased long-range mobility due to the development of high speed trains and large highway systems [39]. It is important to note that this area has never been subjected to overall large-scale planning efforts, one reason being that 14 different administrative bodies preside over 14 different municipalities. By importing historical topographical and photogrammetrical data (for details see the Methods section) into a Geographical Information System (GIS) environment, we reconstructed the detailed road system (including minor streets) at seven different points in time, $t = 1, 2, \ldots, 7$, respectively corresponding to years: 1833, 1914, 1933, 1955, 1980, 1994, 2007. For each time, we constructed the associated primal graph [29], i.e. the graph where the nodes represent street junctions and the links correspond to road segments. The geographical information sources used to construct the primal graphs are reported in Table I.

In Fig. 1a we display the road networks at different times, showing how the initial small separate villages have grown by the addition of new nodes and links, eventually merging together in an homogeneous pattern of streets. We denote by $G_t \equiv G(V_t, E_t)$ the graph at time t, where V_t and E_t are respectively the set of nodes and the set of links at time t. The number of nodes at time t is then $N(t) = |V_t|$, while $E(t) = |E_t|$ is the number of links. By definition, we have $V_t = V_{t-1} \cup \Delta V_t$ and $E_t = E_{t-1} \cup \Delta E_t$, where ΔV_t and ΔE_t are, respectively, the set of new nodes and the set of new links added to the system in the time window $]t-1, t]$. In the following we will study the structure of the graph G_t at different times t, focusing in particular on the properties of the new links. As we will show, a quantitative analysis of the temporal evolution of the system will be able to reveal in particular the existence of two simple mechanisms that drive the evolution of the road network over time.

RESULTS

Characterising the growth of the road network.

The Groane area is basically characterised by an uninterrupted growth in the period under consideration and displays remarkable modifications of the road system. As shown in Fig. 1c, in less than two centuries, the total number of nodes N has increased by a factor of twenty,

Date	Source	Owner	Format
1833	Topographical Map of Lombardy-Venetia Kingdom	Italian Military Geographic Institute	Raster
1914	Map of Italy	Italian Military Geographic Institute	Raster
1933	Map of Italy	Italian Military Geographic Institute	Raster
1955	Aerial Photography Survey	Italian Military Geographic Institute	Raster
1980	Lombardy Regional Map	Lombardy Region	Raster
1994	Lombardy Regional Map	Lombardy Region	Raster
2007	Mosaic of Urban Municipalities Plans	Lombardy Region	Vectorial

TABLE I. List of geographical information sources used to construct the data set.

from the original 255 nodes present at $t = 1$ (year 1833) to more than 5000 nodes at $t = 7$ (year 2007). However, the rate of growth is not constant over time: it is slow from 1833 to 1933, fast from 1933 to 1980, and slow again from 1980 to 2007. These different growth rates are the signature of distinct phases of the urbanisation process, and are strongly related to the growth of the population. We indeed show that the number of nodes N is a linear function of the number of people living in the Groane area (see Fig. 2a) or, in other words, that the average number of people per road intersection in the area remains constant over time.

These results highlight the peculiarity of an area where the population remains almost uniformly distributed in space, and no single urban center stands out over the others. In order to remove the demographic component and focus solely on the road network evolution, we adopt the number of nodes N as the natural internal clock of the system, and we study the change of the network properties as a function of N. The number of links E grows almost linearly with N (Fig. 2b, top), showing that the average node degree $\langle k \rangle(t) = 2E(t)/N(t)$ is roughly constant over time, except for a slight increase from $\langle k \rangle \simeq 2.57$ to 2.8 when going from 1914 to 1980. In the bottom panel of Fig. 2b we report the total network length $L_{tot}(t) = \sum_{e \in E_t} \ell(e)$ (where e denotes a network edge, and $\ell(e)$ its length) which increases over time as

$$L_{tot} \sim N^{\gamma} \tag{1}$$

where $\gamma \simeq 0.54$. Consequently, the average length of links decreases as $N^{\gamma-1}$. This result is consistent with the evolution of almost regular two-dimensional lattices with a peaked link length distribution [29, 40]. Indeed, if we consider a uniform distribution of nodes with density ρ on a two-dimensional surface, the typical link length will be of order $\ell' \sim 1/\sqrt{\rho}$, which implies that the total length grows as $L_{tot} \sim E\ell' \sim \sqrt{N}$, thus giving a value $\gamma = 1/2$.

Additional information on the structure of the road network can be obtained by looking at the quantity [41]

$$r_N = \frac{N_1 + N_3}{\sum_{k \neq 2} N_k} \tag{2}$$

where N_k denotes the number of nodes of degree k (notice that we do not take into account nodes having $k = 2$

in the sum, since these are not usually considered as proper junctions). This quantity r_N measures the relative abundance of dead ends (corresponding to N_1) or T-shaped intersections (N_3), so that a small value of r_N indicates a dominance of $k = 4$ junctions and reveals the presence of a large amount of grid-like patterns. Conversely, the value of r_N is closer to 1 if the network has numerous T-shaped crossings and dead ends. The plot of r_N versus N (Fig. 2c) displays a steady decrease from $r_N \simeq 0.87$ at year 1833 to $r_N \simeq 0.835$ at year 2007, consistent with an increase of the percentage of four-ways crossings from $N_4/N \simeq 11\%$ at year 1833 to $N_4/N \simeq 15.5\%$ at year 2007. Recent studies have shown that the abundance of T-shaped crossings seems to be typical of self-organised or 'organic' urban networks, like those of Venice or Cairo [31], while the grid-like layout is particular to cities whose shapes are the result of large-scale top-down planning efforts [41], like Barcelona or New York. Consequently, one would conclude that what we are observing here is the evolution from an initial self-organised system to a rationally planned urban network. However, the Groane area at $t = 1833$ was actually a fully rural, not urban-organic network, and the successive evolution up to year 2007 has never witnessed any large-scale planning whatsoever. We therefore interpret the result of Fig. 2c as the signature of an evolution from a 'pre-urban' condition, with the dominance of dead-ends and $3-$junctions typical of rural centres in the very early stages of growth (i.e. still constrained by the radial convergence of major roads), to an increasingly mature 'urban' state, in which the network expands on a relatively unconstrained land, further away from the dense radial system of original centres. At that later urban stage the dominance of the $4-$junctions grid-like pattern does not result from large-scale planning, but from a piecemeal urbanisation, made of a multitude of small-scale, plot-based, scarcely coordinated developments in time, i.e. a substantially self-organised territorial order.

Evolution of cells: towards homogenisation.

Road networks are planar graphs consisting of a series of land cells surrounded by street segments. The statistics on the area and the shape of cells can be used to distinguish regular lattices from heterogeneous patterns. In particular, it has been recently observed that for Dresden
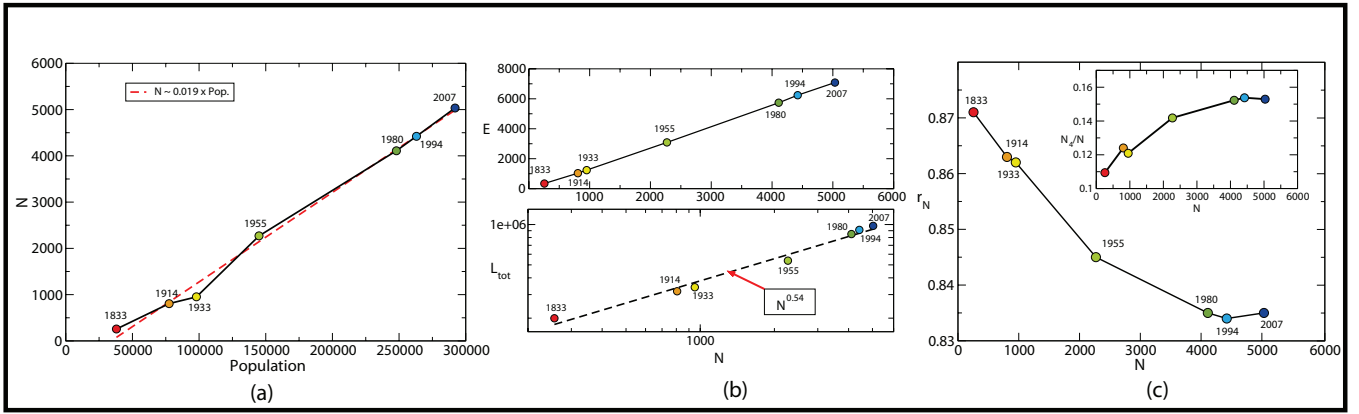
FIG. 2. **(a)** Number of nodes N versus total population (continuous line with circles) and its linear fit (red dashed line). **(b)** Total number of links E and total network length L_{tot}, as a function of the number of nodes N. The total network length increases as $N^{0.54}$. **(c)** Value of the ratio r_N between the number of nodes with degree $k = 1$ and $k = 3$, and the total number of nodes. In the inset we report the percentage of nodes having degree $k = 4$ as a function of N. Notice that the relative abundance of four-ways crossings increases by 5% in two centuries.

(Germany)[30] and for a simple model of road networks [40], the cell area distribution $P(A)$ is a power law

$$P(A) \sim A^{-\tau} \qquad (3)$$

with an exponent τ very close to the value 1.9. This value of τ can be explained in terms of a lattice constructed on a set of nodes with density fluctuations [29]. In Fig. 3a we report the distribution of the cell size in the Groane area at $t = 2007$, which is indeed a power law with the same exponent $\tau = 1.9 \pm 0.1$. However, the exponent changes in time, as reported in the inset: it takes a value $\tau \simeq 1.2$ at year 1833 and converges towards $\tau \simeq 1.9$ as the network grows. Because a larger exponent indicates a higher homogeneity of cell areas, we are thus witnessing here a process of homogenisation of the size of cells. Accordingly, the relative dispersion $\delta_A = \sigma(A)/\mu(A)$ of cell areas (where $\mu(A)$ and $\sigma(A)$ are the average and the standard deviation of A, respectively) decreases from 0.5 at year 1833 to 0.26 at year 2007, indicating that the variance of the distribution becomes smaller as N increases.

The diversity of the cell shapes can be quantitatively characterised by the so-called shape factor $\Phi = A/(\pi D^2/4)$, defined as the ratio between the area A of a cell and the area of the circle of diameter D circumscribed to the cell [26]. The value of the shape factor is in general higher for regular convex polygons, and tends to 1 when the number of sides in the polygon increases. The distributions $P(\Phi)$ reported in Fig. 3b clearly reveal the existence of two different regimes: before 1933 the distributions are single-peaked and well approximated by a single Gaussian function with an average of about 0.5 and a standard deviation of 0.25. Conversely, after 1955 the distributions of the shape factor display two peaks and can be fitted by the sum of two Gaussian functions. The first peak coincides roughly with the one observed before 1933, while the second peak, centred at 0.62, signals the appearance after 1955 of an important fraction of regular

shapes, such as rectangles with sides of similar lengths. In Fig. 3c-d we show the cell shapes at different times (before and after 11955) which visually confirm the findings of Fig. 3. The decrease in the relative dispersion δ_A and the increase in the fraction of regular shapes suggest that the network undergoes an evolution towards homogenisation. This appears to result from a combined process that exhibits two clear patterns: *i)* the fragmentation of larger cells of natural land into smaller ones, then heading towards urbanisation by medium-large manufactures or services, and *ii)* the mostly residential urbanisation of peri-urban natural land in successive rings around the historical urban centres. In particular, this latter pattern explains the emergence of more regularly shaped cells after the Second World War. As urbanization took place increasingly further from historical main roads, residential blocks became less constrained by the triangular shape defined by those roads and, as a result, increasingly followed a regular rectangular shape. This regular shape is in fact the most efficient way of subdividing land for urbanization, reflecting the inner organization of the block into equally regular rectangular plots. This grid-like layout tends to be applied extensively when local constraints, like main roads converging into a village, do not force the development along different patterns (for example T-shaped junction dominated) [42].

Properties of new links: elementary processes of urbanisation.

Road networks grow by the addition of new streets (links) and new junctions (nodes). We focus here on the properties of new links by looking at their length and centrality. In Fig. 4 we show the cumulative distribution of the length of new links according to the time-section in which they appeared first. The inset shows that the
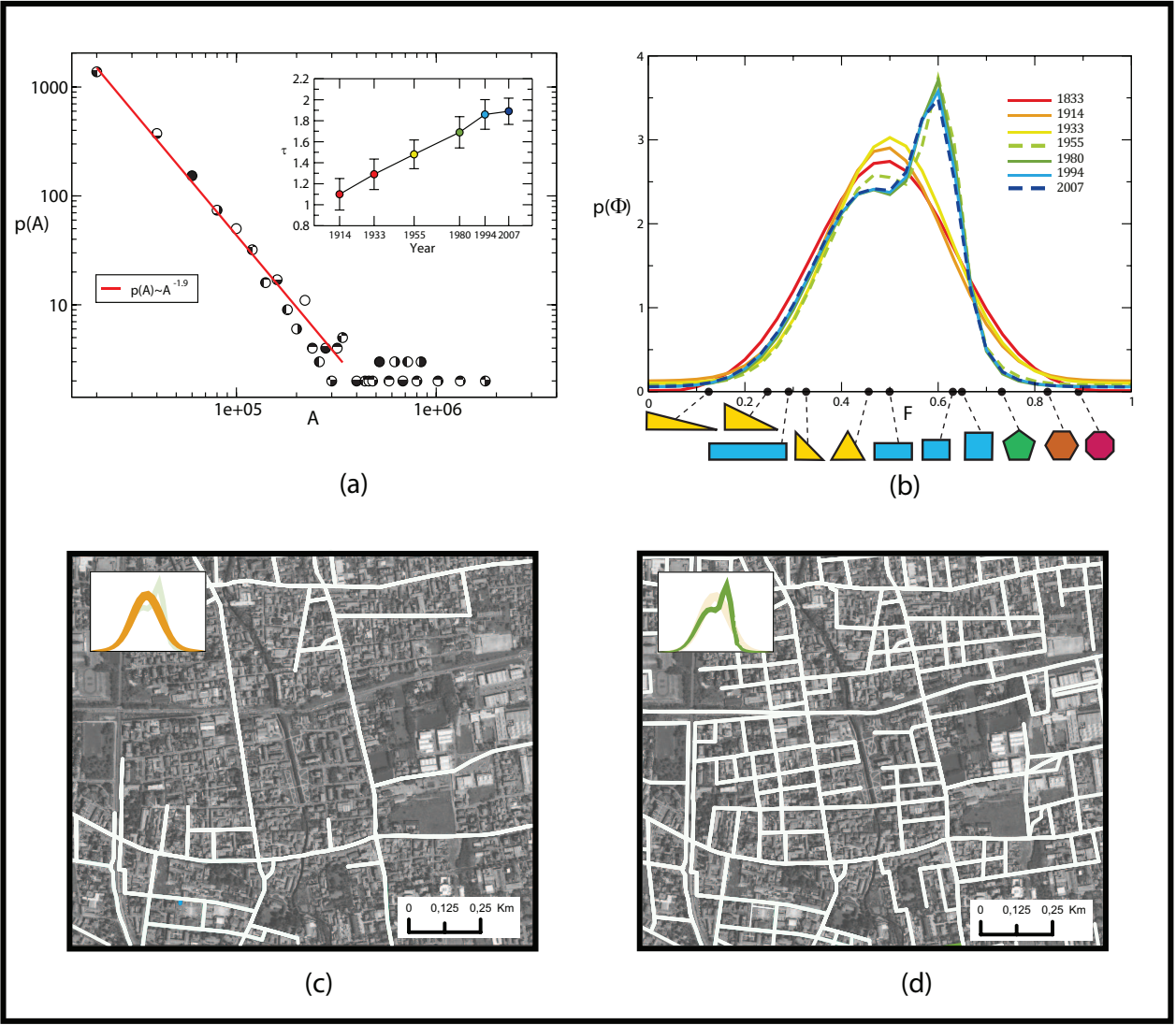
FIG. 3. **(a)** The size distribution of cell areas at $t = 2007$ can be fitted with a power-law $p(A) \sim A^{-\tau}$, with an exponent $\tau \simeq 1.9$. The inset shows the value of τ at different times. **(b)** Distribution of cell shapes at different times, as quantified by the shape factor Φ. The shape factor of different polygons is reported at the bottom axis for comparison. **(c)** and **(d)** Maps showing the cell shapes (white lines) for the network as it is before 1955 (left panel) and as it is after 1955 (right panel). We see on the left panel that we have predominantly triangles and rectangles, while on the right panel we can observe a predominance of rectangles with sides of almost the same length.

average length of new links steadily decreases over time, as expected from the general considerations of land fragmentation reported above. More precisely, we consider, at each time t, the length value $\ell_{90\%}(t)$ such that 90% of new links at time t are shorter than $\ell_{90\%}(t)$ (i.e. such that $P(\ell \leq \ell_{90\%}) = 0.9$). We notice that the value $\ell_{90\%}$ decreases in the period 1833-1933 from 625 meters down to 325 meters, while no sensible variation is observed from 1933 to 1994, even if the network keeps growing. In the last period, i.e. from 1994 to 2007, we observe another decrease of $\ell_{90\%}(t)$ from 325 to 225 meters. In addition, the relative dispersion of the length of the new links is almost constant and of order one, and the distribution does not vary too much after 1955. This phasing fits

well with the historical development outlined in the introduction where during the rural and early-urban phase up to the second world war we observe the passage to an urban state that is then maintained along the core urbanisation age in the urban-industrial period until the 1980s, followed by a different post-industrial, metropolitan regime.

The nature of the growth process can be quantitatively characterised by looking at the centrality of streets. Among the various centrality indices available for spatial networks, we use here the betweenness centrality (BC) [43–45], which is one of the measures of centrality commonly adopted to quantify the importance of a node or a link in a graph. Given the graph $G_t \equiv G(V_t, E_t)$ at time
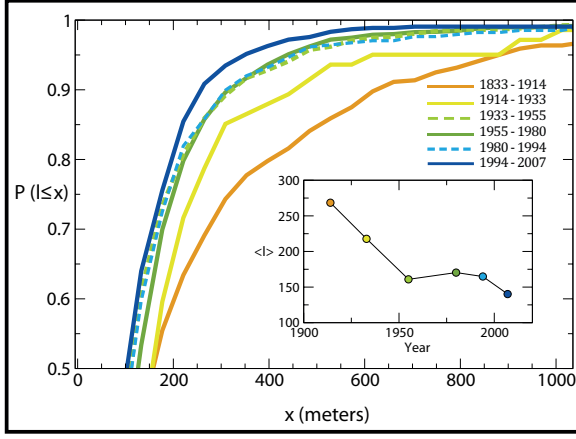
FIG. 4. Cumulative distributions of the length of links added at different times. In the inset we report the average length $\langle \ell \rangle$ of new links.

t, the BC of a link e is defined as

$$b(e) = \sum_{i \in V} \sum_{\substack{j \in V \\ j \neq i}} \frac{\sigma_{ij}(e)}{\sigma_{ij}} \qquad (4)$$

where σ_{ij} is the number of shortest paths from node i to node j, while $\sigma_{ij}(e)$ is the number of such shortest paths which contain the link e. The quantity $b(e)$ essentially measures the number of times a link is used in the shortest paths connecting any pair of nodes in the network, and is thus a measure of the contribution of a link in the organisation of flows in the network. In order to evaluate the impact of a new link on the overall distribution of the betweenness centrality in the graph at time t, we first compute the average betweenness centrality of all the links of G_t as:

$$\bar{b}(G_t) = \frac{1}{(N(t)-1)(N(t)-2)} \sum_{e \in E_t} b(e) \qquad (5)$$

where $b(e)$ is the betweenness centrality of the edge e in the graph G_t. Then, for each link $e^* \in \Delta E_t$, i.e. for each newly added link in the time window $]t-1, t]$ we consider the new graph obtained by removing the link e^* from G_t and we denote this graph as $G_t \setminus \{e^*\}$. We compute again the average edge betweenness centrality, this time for the graph $G_t \setminus \{e^*\}$. Finally, the impact $\delta_b(e^*)$ of edge e^* on the betweenness centrality of the network at time t is defined as

$$\delta_b(e^*) = \frac{[\bar{b}(G_t) - \bar{b}(G_t \setminus \{e^*\})]}{\bar{b}(G_t)} \qquad (6)$$

The BC impact is thus the relative variation of the graph average betweenness due to the removal of the link e^*. We have measured this quantity for the different times-section and we report the results in Fig. 5. Remarkably, the distribution of $\delta_b(e)$ displays two well-separated peaks (Fig. 5d). The importance of the first peak tends to increase in time while the second peak decreases, until they mostly merge into one single peak in the last time-section (1994-2007). In order to understand the nature and the evolution of the two peaks, we focus on the geographical location of new links with different BC impact.

In Fig. 5a-c we report, respectively, the map of the network at year 1914, year 1994 and year 2007. We have coloured in green the links whose centrality impact belongs to the left peak, and in red the links whose δ_b corresponds to the right peak. The new links are divided into two classes: green links (small δ_b, left peak) tend to bridge already existing streets, while red links (large δ_b, right peak) are usually dead-ends edges branching out of existing links, generating a new crossing and splitting the original link into two road segments. In order to better characterise the two classes of edges we compute $k_{min}(e)$, i.e. the minimum of the degrees of both endpoints of a new link e, and we then consider, for each value of δ_b, the relative abundance of new links for which k_{min} is equal to $1, 2, 3, 4$, respectively. We plot the results in a gray–scale stacked chart (see Fig. 5e) for the network at year 1955 (the plots for the other networks are similar). The analysis of k_{min} confirms that the links belonging to different peaks have distinct qualitative features: links in the right peak have $k_{min} = 1$, while links in the left peak have $k_{min} \geq 2$. The distribution of BC impact thus suggests that the evolution of the road network is essentially characterised by two distinct, concurrent processes: one of *densification* (green links, left peak, i.e. lower impact on centrality, $k_{min} \geq 2$) which is responsible for the increase of the local density of the urban texture, and one of *exploration* (red links, right peak, higher impact on centrality, $k_{min} = 1$) which corresponds to the expansion of the network towards previously non-urbanised areas. At a closer sight, these two patterns tend in many cases to appear in a temporal sequence, the former acting in preparation for the latter, i.e. exploration being the first phase of a cycle of urbanisation then completed by a second phase of densification. Obviously, since the amount of available land decreases over time, at earlier time–sections (such as in the year 1914) the fraction of exploration is higher, while in the 80's it becomes smaller until it almost disappears in 2007. The only remaining peak mostly corresponds to densification with new links having $k_{min} \geq 2$.

We finally focus on another aspect of the evolution of street centrality, namely the relation between the age of a street and its centrality. In Fig. 6a we display the links of the network in 2007 with a color code depending on their age, and in Fig. 6b we report their BC. A simple visual inspection shows that highly central links usually are also the oldest ones. In particular, the links constructed before 1833 have a much higher centrality than those added at later time–sections. More precisely, the seven curves in panel Fig. 6c report the cumulative distribution of the BC computed on the network in 2007 for the links added at the different times. This is defined as the probability
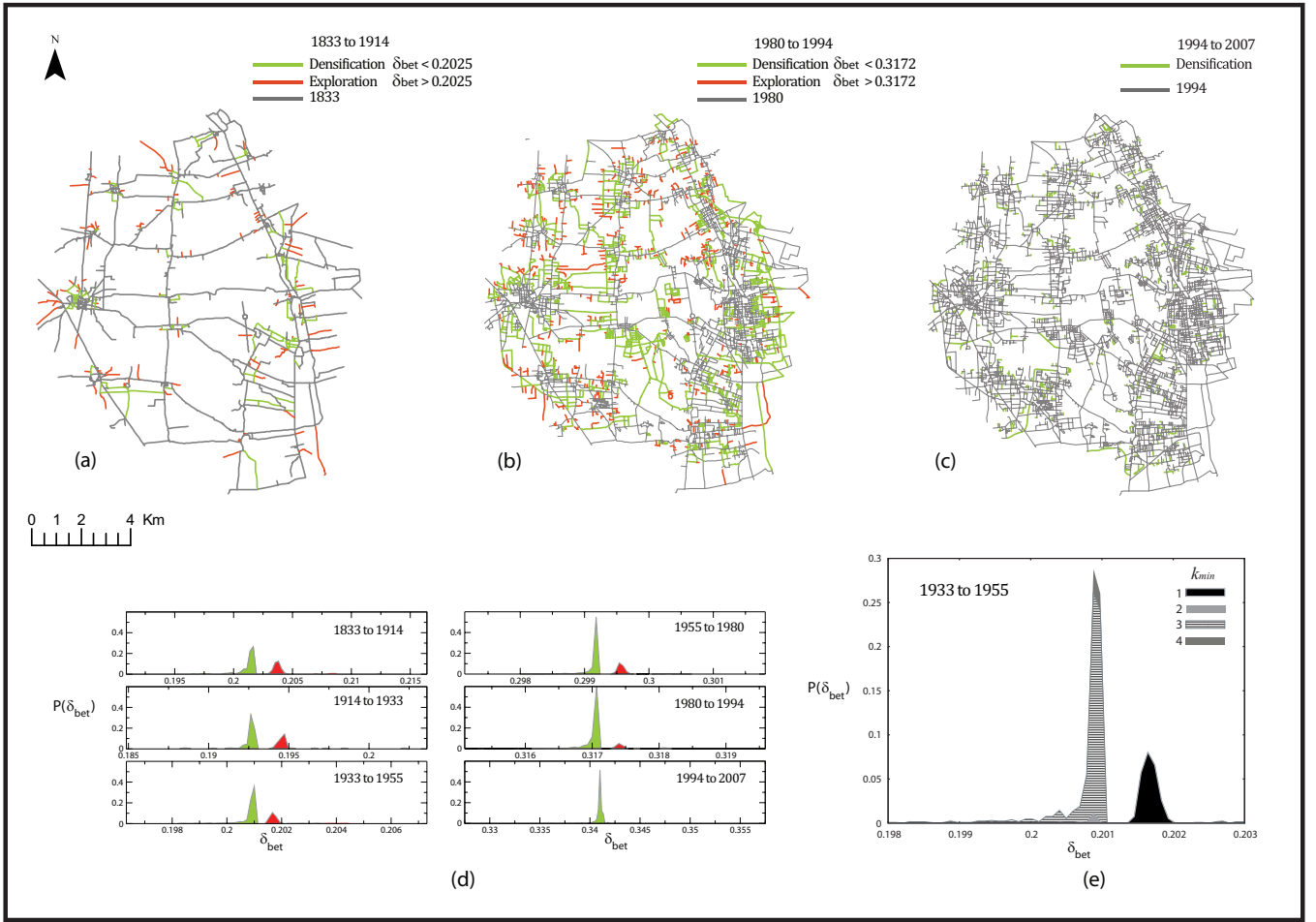
FIG. 5. The two phases of densification (green) and exploration (red), illustrated for the networks at year 1914 **(a)**, 1994 **(b)** and 2007 **(c)**. Panel **(d)** shows the probability distribution of the BC impact $\delta_b(e)$ for the different time snapshots. The red peak corresponds to exploration, and the green peak to densification. Notice that the red peak becomes smaller and smaller with time, and completely disappears in the last snapshot. **(e)** Stacked chart showing the proportion of new links with a certain value of k_{min} for each value of δ_b in the network at $t = 1955$. The peak corresponding to exploration with a high BC impact is entirely due to links having $k_{min} = 1$.

$P(b \leq x)$ that a link, appearing at a certain time-section, has a value of betweenness centrality b smaller than or equal to x in the final network in 2007. We notice that the historical structure of the oldest roads mostly coincide with the highly central links at year 2007. In particular, the inset of Fig. 6c indicates that more than 90% of the 100 most central links in 2007 (and almost 60% of the top 1000) were already present in 1833. This result reveals that a "backbone" of highly–central routes, that have framed the Groane area in the rural economy of the pre-industrial period, has been driving the development of the area across two centuries of industrialisation, urbanisation and de-industrialisation up to present days, without any major modification.

Urban morphologists have long observed that streets tend to persist in time much longer than other urban elements like buildings or land-uses [47]. Our results confirm that at another level, that of the topology of the street network, the persistence of roads over time appears to

be due to their multifaceted impact on the urban form at different scales by deeply informing factors like accessibility to space and resources, land ownership and land values, each of these involving different social actors and interests.

DISCUSSION

In this paper we have studied the evolution, over almost two centuries, of the street network in a large large area close to Milan (Italy). Such an area is of interest for urban studies because it displays an important process of urbanisation. Urbanisation is reflected in the growth of the road network and displays different speeds at different times, with a fast increase occurring between 1933 and 1994. Our results reveal a quantitative signature of urbanisation on the evolution of the shape and size of land cells, which become more homogeneously dis-
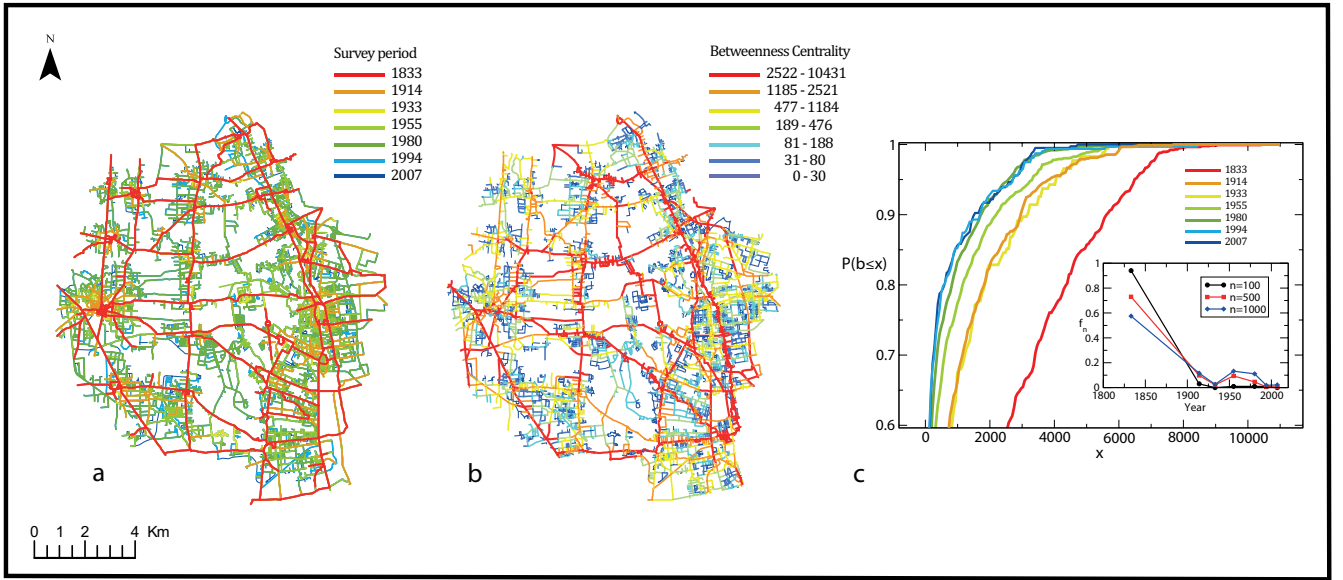
FIG. 6. Color maps indicating **(a)** the time of creation of each link and **(b)** its value of betweenness centrality (BC) at year 2007. **(c)** The cumulative distribution of BC of links added at different times. The inset reports the percentage of edges added at a certain time which are ranked in the top n positions according to the BC. Different curves correspond to $n = 100, 500, 1000$.

tributed and square-shaped. Simultaneously, we observe a general trend towards a larger number of 4-way junctions, as opposed to an earlier structure of dead ends and 3-way junctions. These structural transformations appear to be the result of the interplay between two concurrent dynamics, namely densification and exploration. While exploration is typical of the earliest historical periods of urbanisation, densification predominates in the latest.

We were also able to quantitatively characterise the stability of the structure of most central streets over time. For instance, the most central streets in the network in 2007 largely coincide with the oldest ones. Central roads appear to therefore constitute a robust spatial backbone which remains stable over time, and characterises the evolution of the road system as a continuous expansion and reinforcement of pre-existing structures rather than as a sharp switch towards radically new configurations. The kind of evolution that we are witnessing in the Groane area is therefore certainly massive in overall quantitative terms, reflecting unparalleled changes in the pace and nature of economic, technological and social order during the transition from a mainly agricultural to a post-industrial age; however, it is still an organic form of evolution that builds at each step on the achievements of the previous, confirming in the long term a resilient structure that tends to persist in time all over the urbanisation process. These findings quantitatively support the hypothesis that spatial systems undergoing fine-grained forms of evolution tend to exhibit simple local dynamics of change, continuously expanding upon pre-existing structures, a morphogenetic behaviour that they appear to share with many living organisms and other natural systems [46].

The results of this research, including the existence of the two main dynamics of exploration and densification, together with the persistence over time of a structural backbone made of highly central streets, cannot be extended to the generality of urbanisation processes unless supported by further investigation of cases in different geographical and economic positions. An important point in our view is that this study provides quantitative results which can be confirmed (or falsified), a critical aspect in Science.

METHODS

Temporal Network Data.

The area under study covers 125km^2 and includes 29 urban centers within 14 municipalities that have developed along two main radial paths, connecting Milan to Como and Milan to Varese. We sampled seven street networks primal graphs at different times, where the street junctions are represented as nodes and the roads (or streets) are the links of the networks. We used a mixed procedure of ArchMap tool extensions and python scripts operating over a geo-database. First, the street network has been drawn in vectorial format on the basis of a collection of historical areal images and historical maps imported in the ArcGIS10 platform. Sources used for each temporal steps are reported in Table 1. The images have been imported as a .geotif extension, and all the layers has been projected using the coordinate system Monte Mario (Rome), Italy zone and Transverse

Mercator projection. The first geo-referencing (alignment of different images) has been performed on the basis of historical buildings and landmarks such as paths and roads. The redraw operation was done using an ad-hoc python script for creating the node layers representing the street junctions. The second geo-referencing operation has been performed over the street junctions using the spatial analyst tool with the spatial join utilities provided in ArchMap10. Subsequently, for all time layers, using an ad-hoc python script we produced the weighted adjacency lists that has been used for the network analysis, the weight correspond to the real length of the street. We denote by $G_t \equiv G(V_t, E_t)$ the obtained primal graph at time t, where V_t and E_t are respectively the set of nodes and links at time t. The number of nodes at time t is then $N(t) = |V_t|$ and the number of links is $E(t) = |E_t|$. Using common definitions, we thus have $V_t = V_{t-1} \cup \Delta V_t$ and $E_t = E_{t-1} \cup \Delta E_t$, where ΔV_t and ΔE_t are respectively the new street junctions and the new streets added in time $]t-1, t]$ to the network existing at time $t-1$.

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All the authors have equally contributed to the design of the experiment, to the analysis and interpretation of the results and to the preparation of the manuscript.

ADDITIONAL INFORMATION

Competing financial interests

The authors declare no competing financial interests.